

# Looking forward and benefiting from the past: Sample size estimation for new arms in platform trials

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**EU-PEARL**  
EU AND PARTNER CENTRIC  
COOPERATION FOR TB DRUG DEVELOPMENT



This project has received funding from the Innovative Medicines Initiative 2 Joint Undertaking (JU) under grant agreement No 853966. The JU receives support from the European Union's Horizon 2020 research and innovation programme and EFPIA and CHILDREN'S TUMOR FOUNDATION, GLOBAL ALLIANCE FOR TB DRUG DEVELOPMENT NON PROFIT ORGANISATION, SPRINGWORKS THERAPEUTICS INC.

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New treatment: How can data already collected be utilized to “optimize” the trial?

- **For test decision?**

- Use of nonconcurrent controls (*Bofill et al., 22*)
- Modification of testing strategy, e.g. outcome of former treatments influences significance boundaries, e.g., online control of FWER, FDR (*Javanmard et al. 15, Tian et al. 21*)

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- **For sample size calculation?**

- Effect size estimation
- Variance estimation
- Significance level

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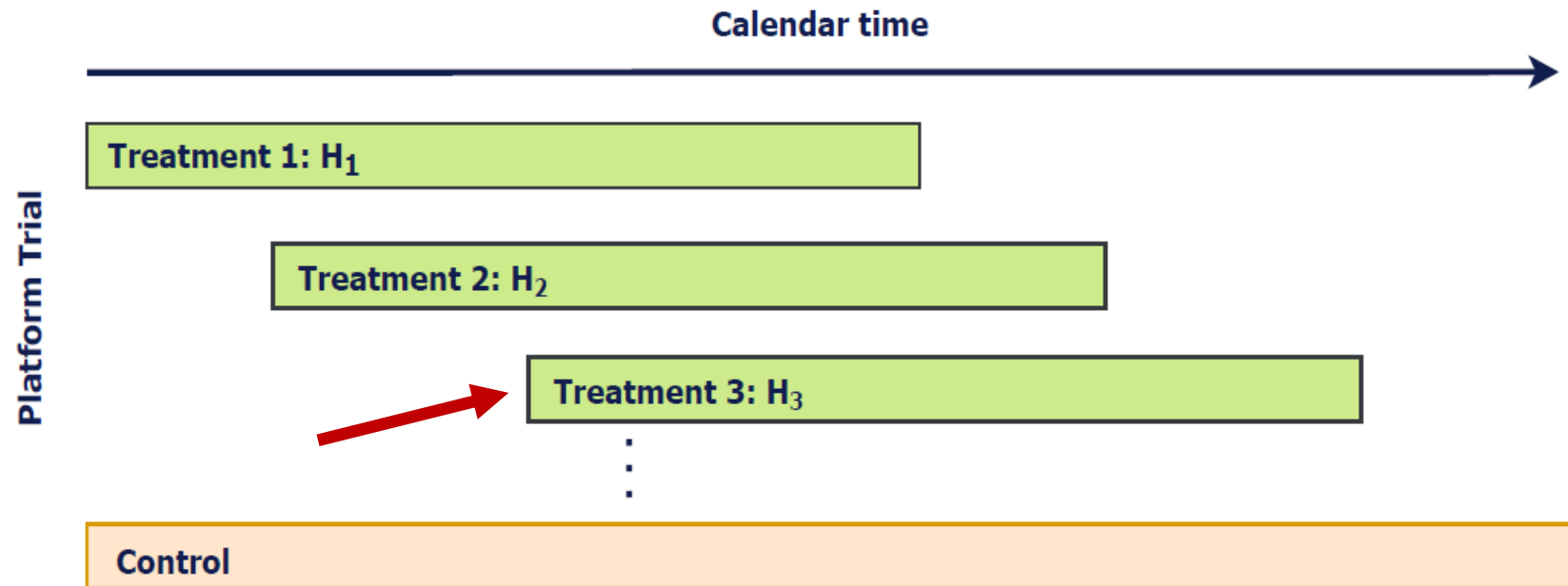
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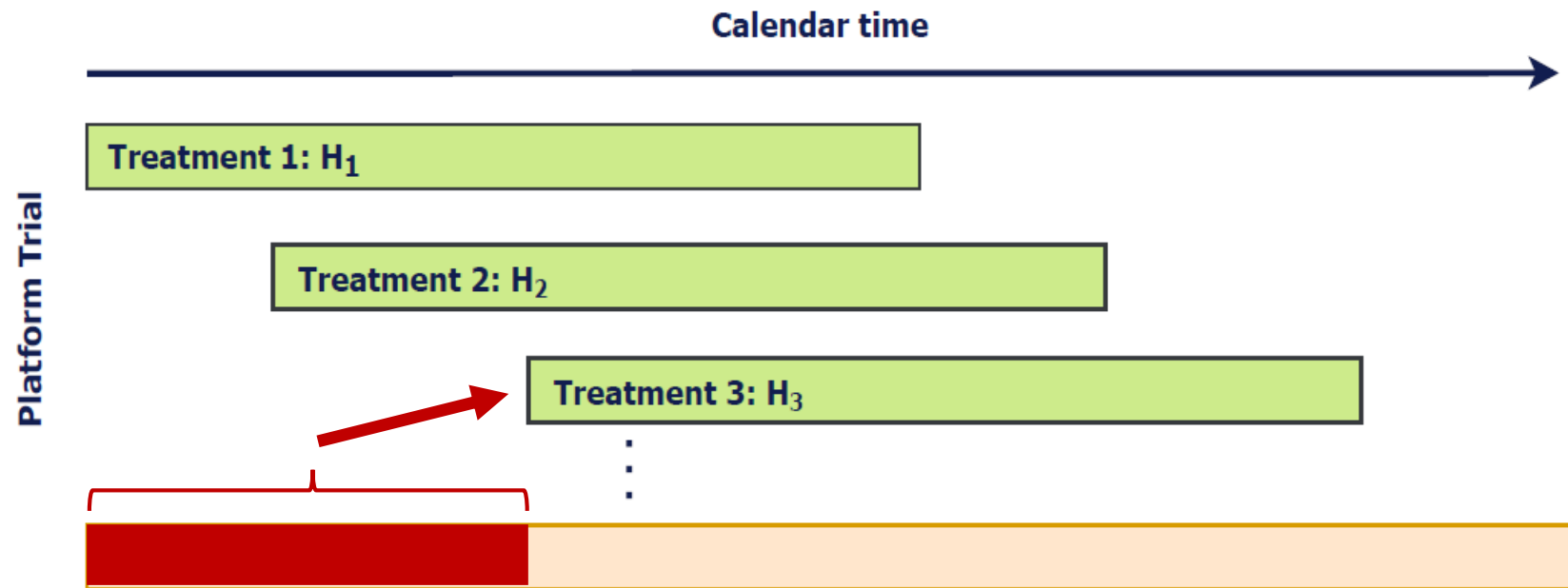
## How is this different to historical data?

- Same definition of endpoints
- Same centers and study population
- Same inclusion and exclusion criteria
- ....

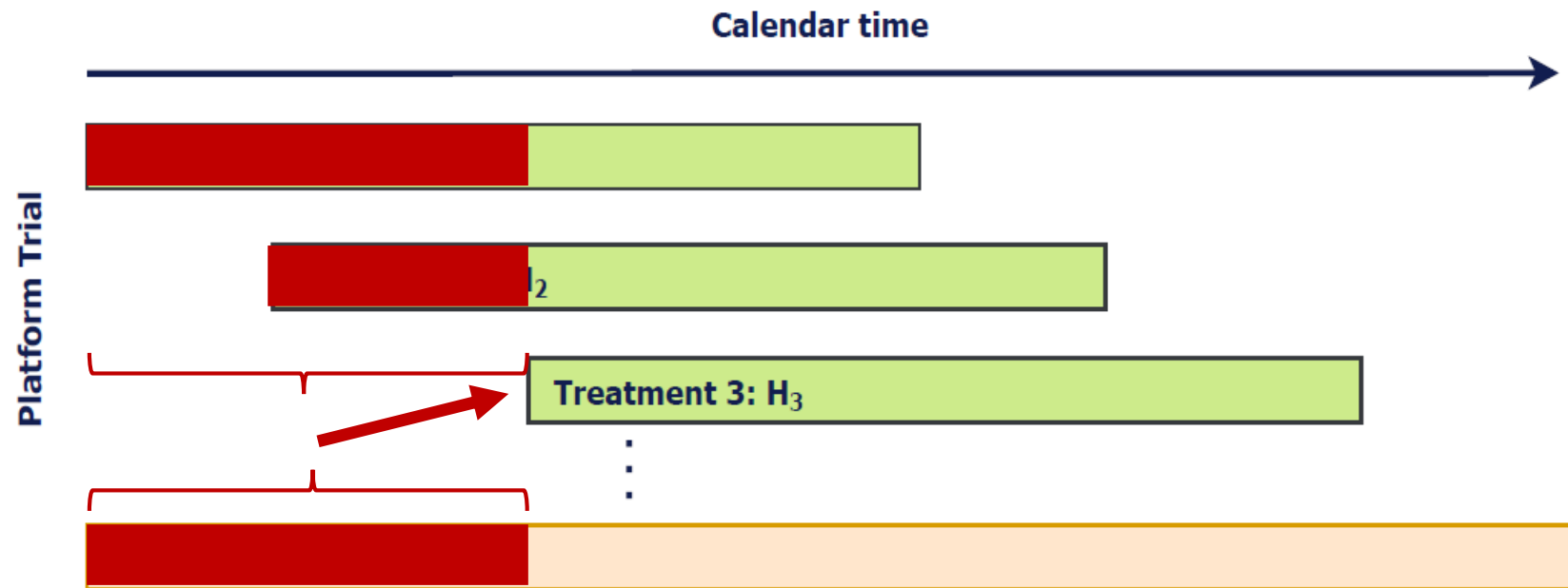
# What about sample size calculation for new treatment arms in platform trials?



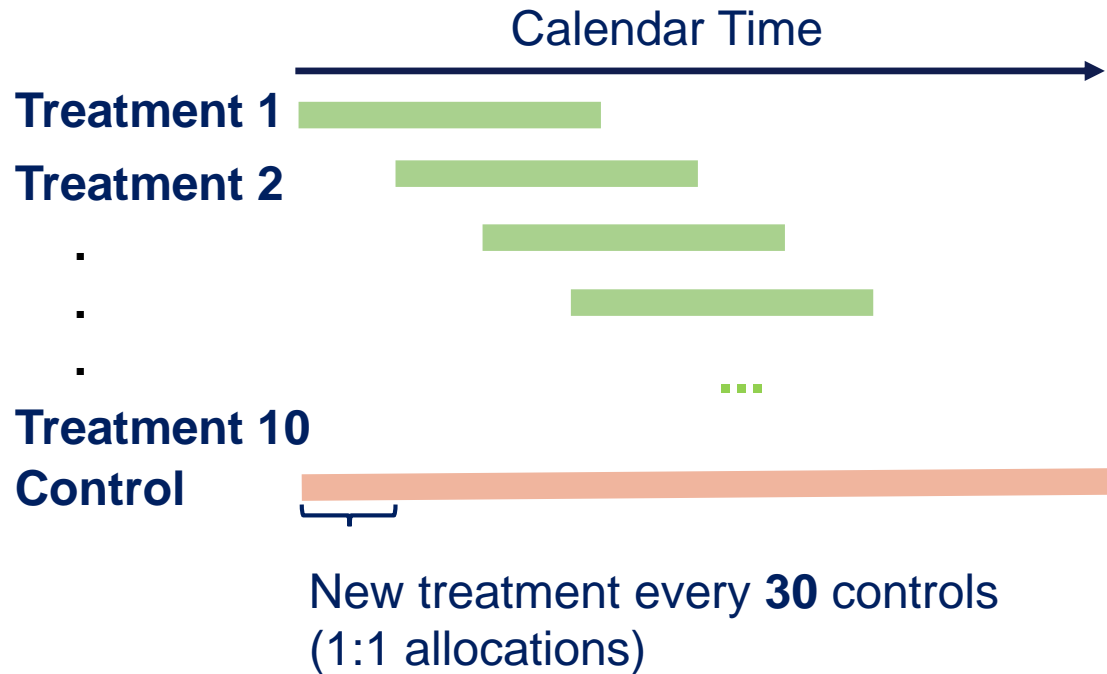
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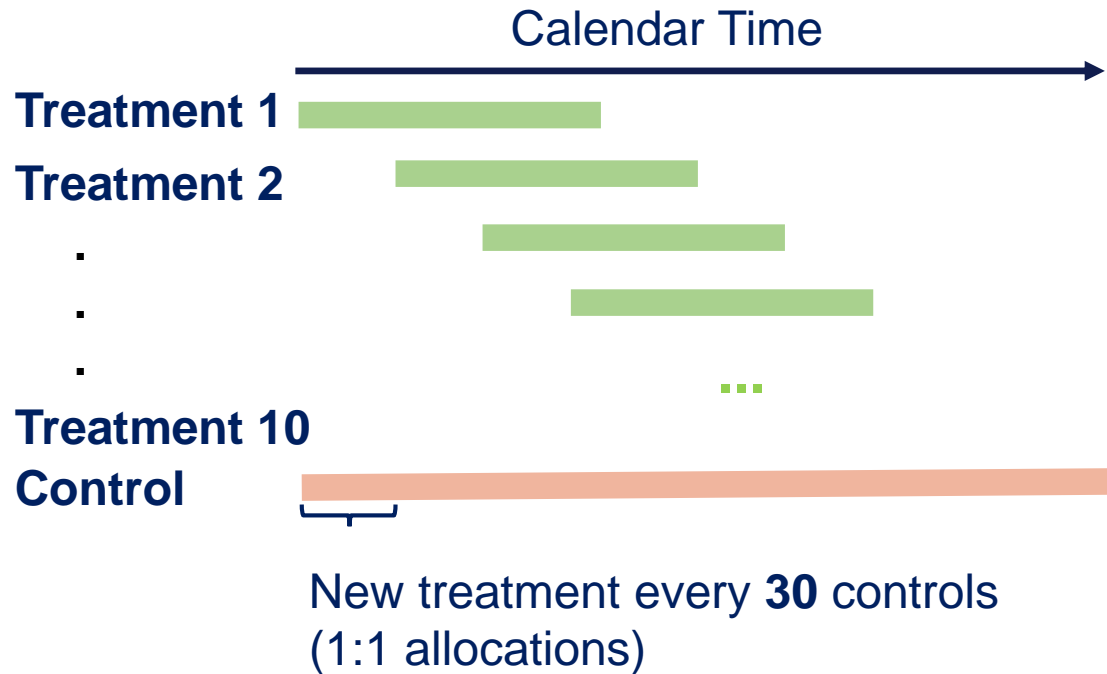
# Sample size calculation with an oracle



- $N(0,1)$  data, for alternatives  $N(\Delta=0.5,1)$
- T-test
- Concurrent controls for test decision
- $\alpha=0.025$  (one-sided)
- Level- $\alpha$  tests (e.g., *Collignon et al., 20*)
- Target average power of 0.8



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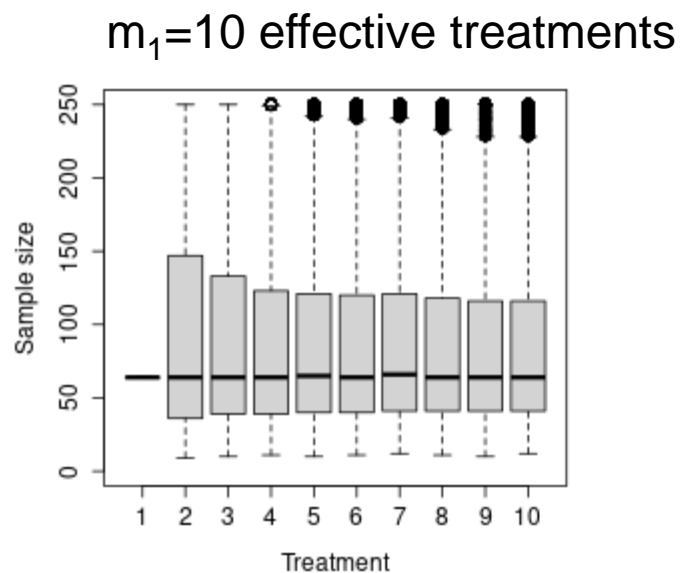


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If an oracle tells us the true parameters: Sample size of each treatment arm: **n=64**

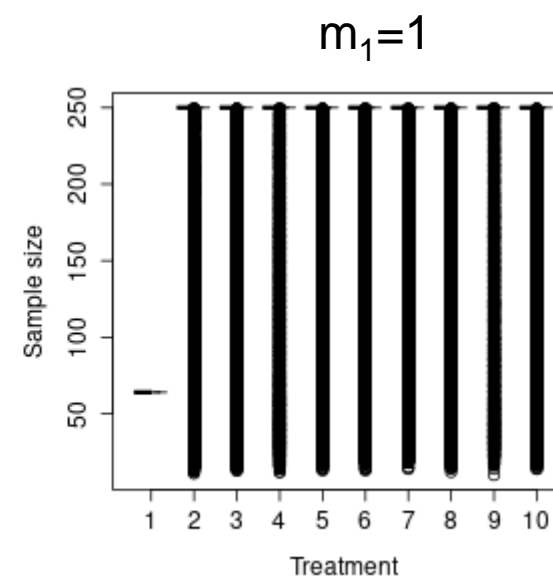
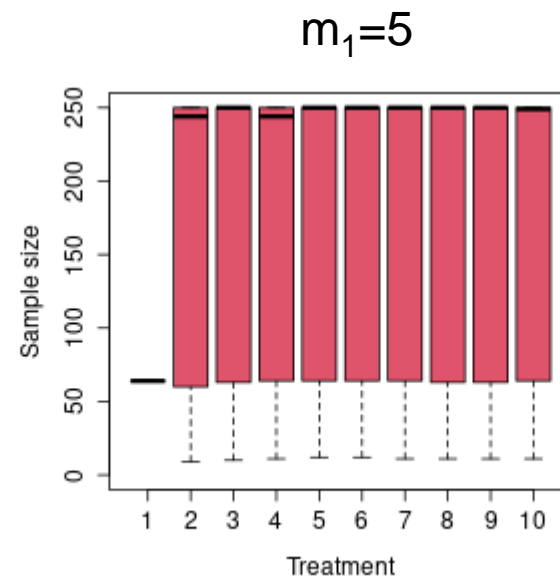
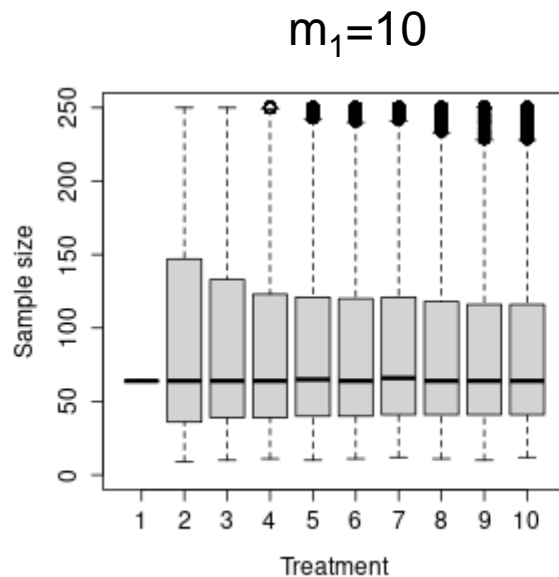
# Naive strategy: Estimate Delta from the observed effect of last treatment and all controls

- Minimum Delta=0.25 (i.e., maximum sample size of 250). Set sd=1
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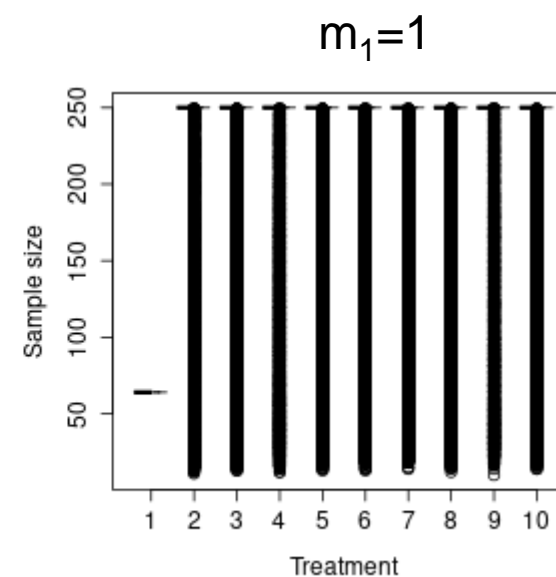
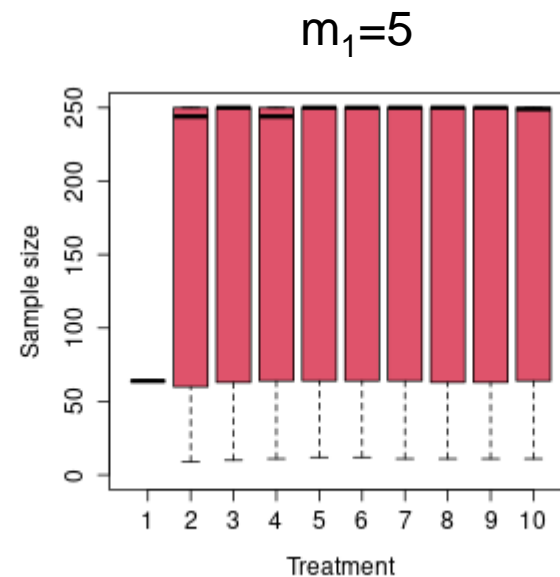
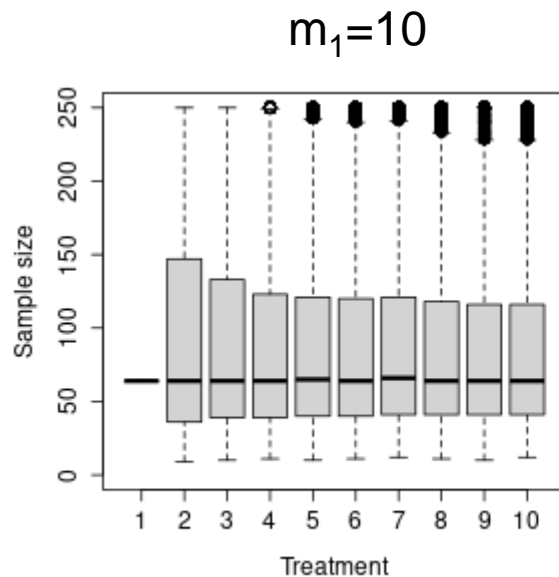


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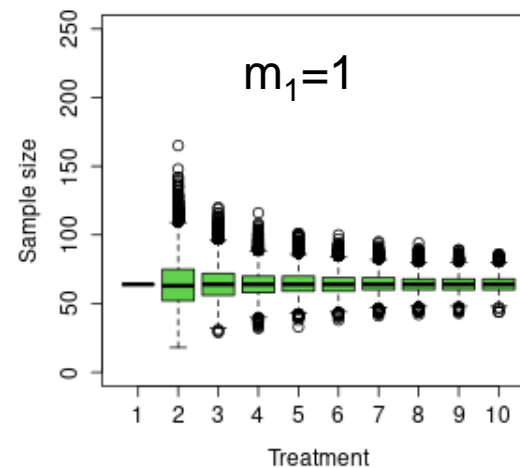
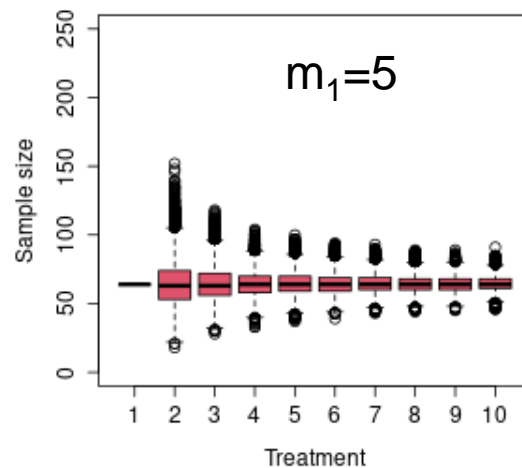
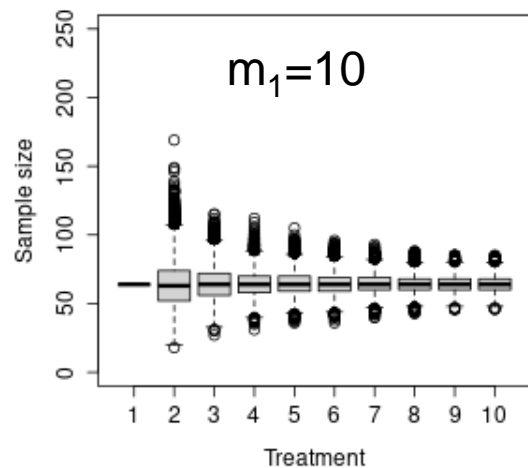
**Why should the effect size of interest depend on the (random) outcome of the former treatment?**

**Set Delta to clinical relevant effect size = 0.5.**



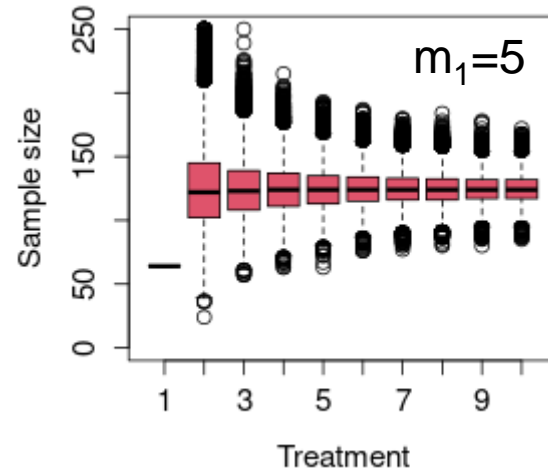
# Estimate standard deviation

- Set  $\Delta=0.5$  (clinical relevant effect size), true  $sd=1$
- Estimate standard deviation from all so far observed controls
  - Range of sample sizes decreases with time
  - The more data we observe, the more precise is the sample size calculation



# False assumption - estimate standard deviation from observed controls

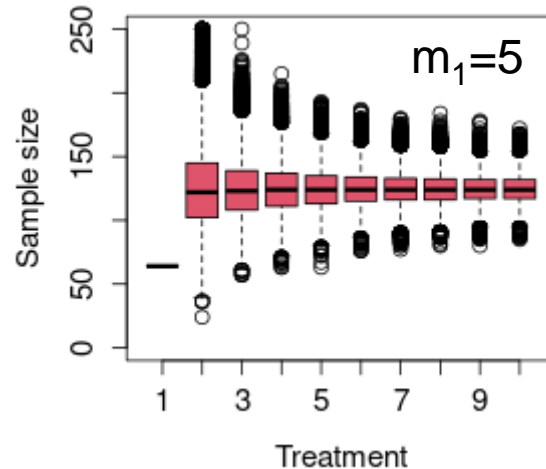
- Assume  $sd=1$  but true  $sd=1.4$



Average power for  
the scenarios = **0.77**

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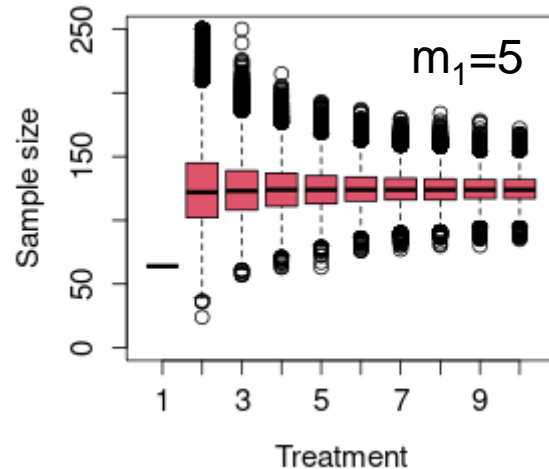


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What happens if we start a new treatment after every 5 controls (instead of 30)?

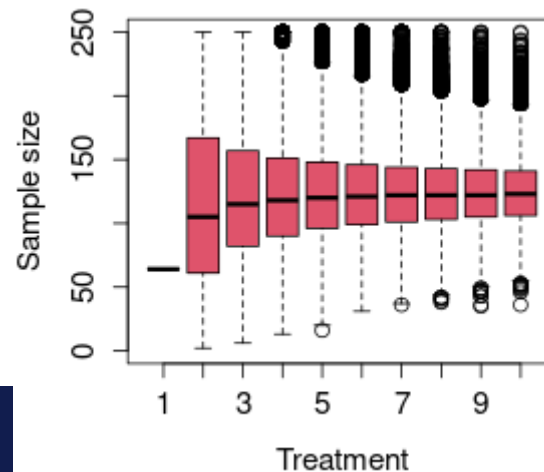
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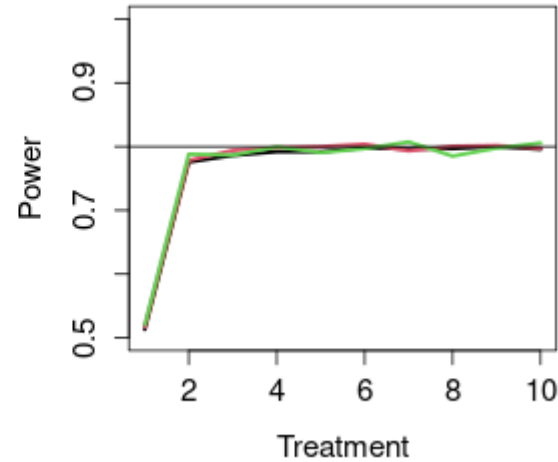
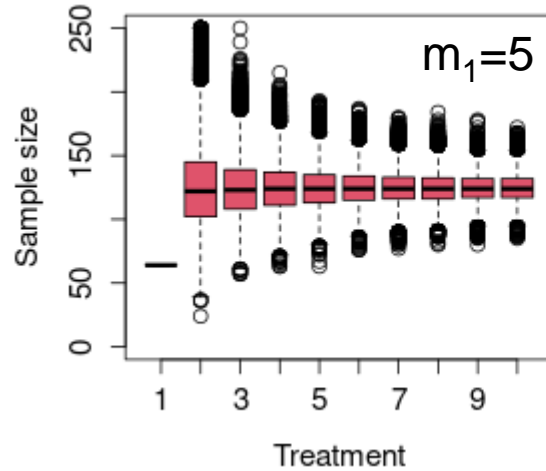


Average power for  
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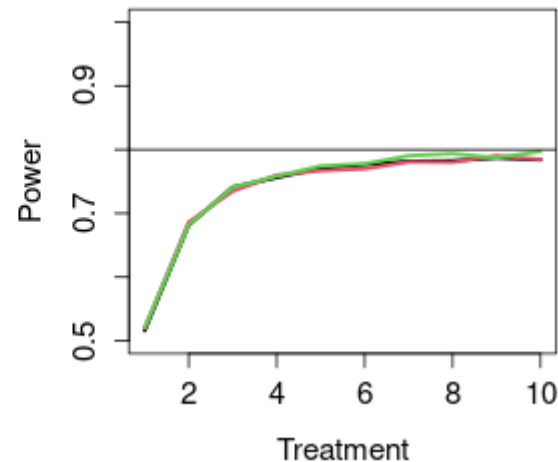
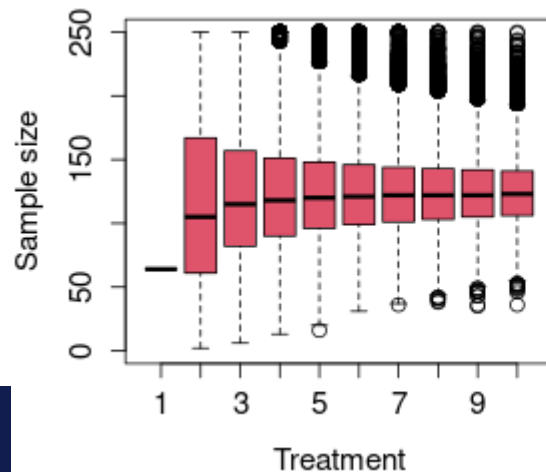


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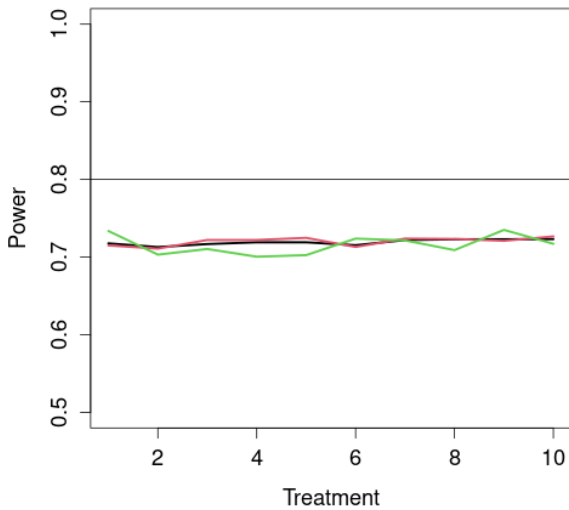


# Heteroscedasticity: Treatment arms with higher variation

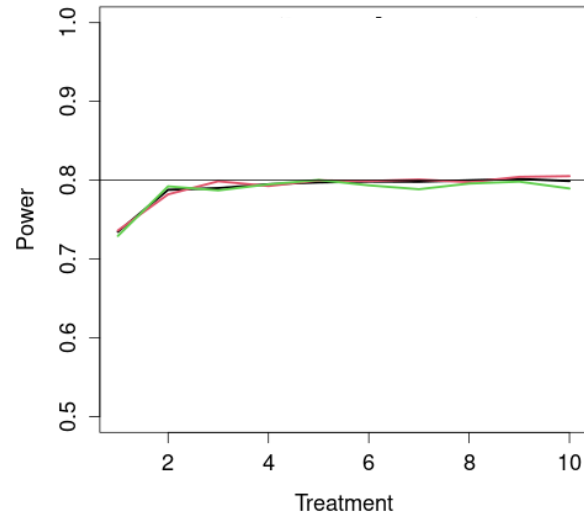
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Estimate sd from data

From controls



From controls and treatments

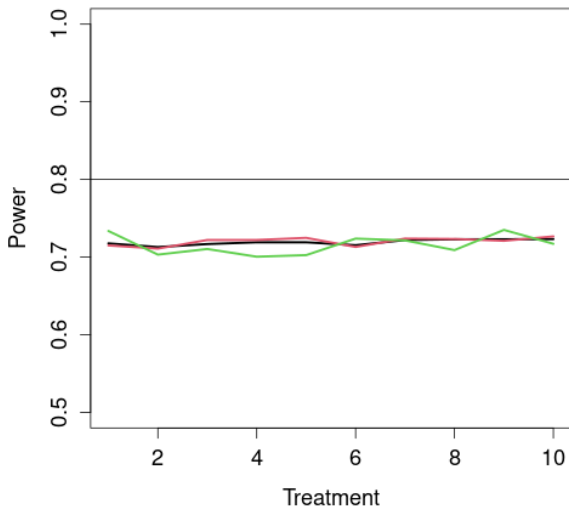


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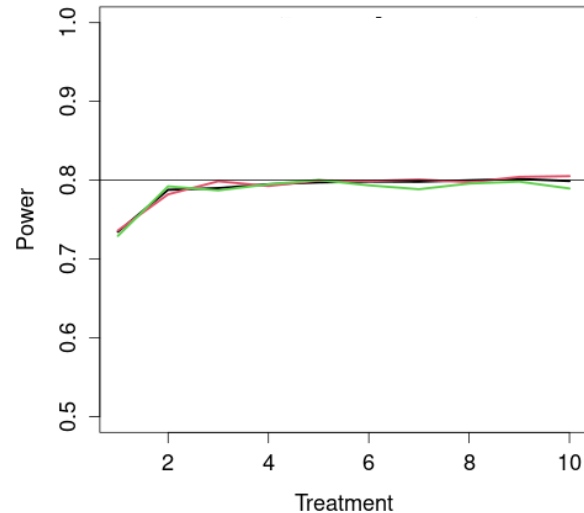
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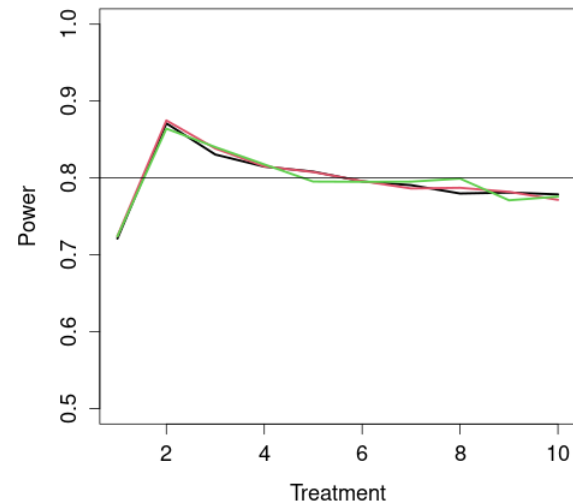


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Estimate sd with CI

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*Wassmer and Kieser, 96*: Use upper CI of sd from pilot sample

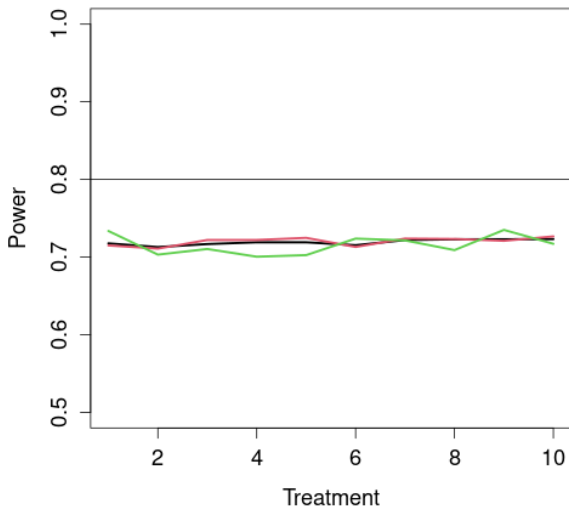
For early treatments, broad CI due to smaller number of previous observations.

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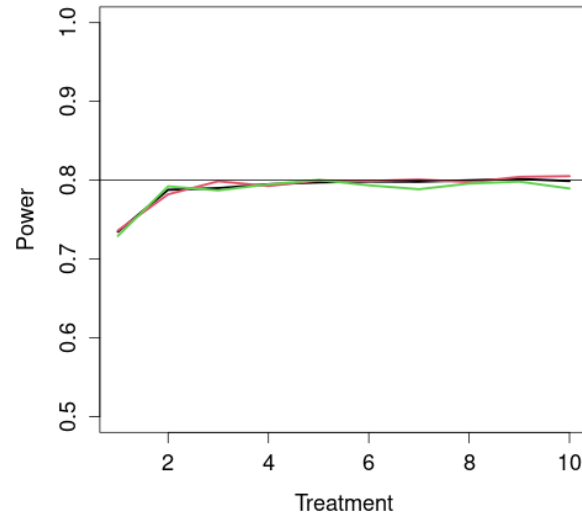
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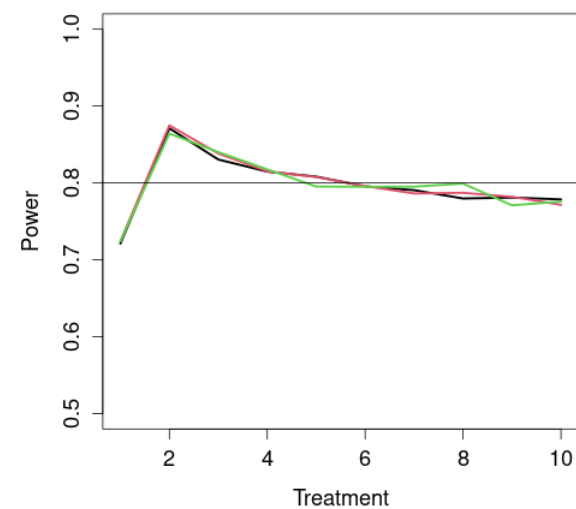


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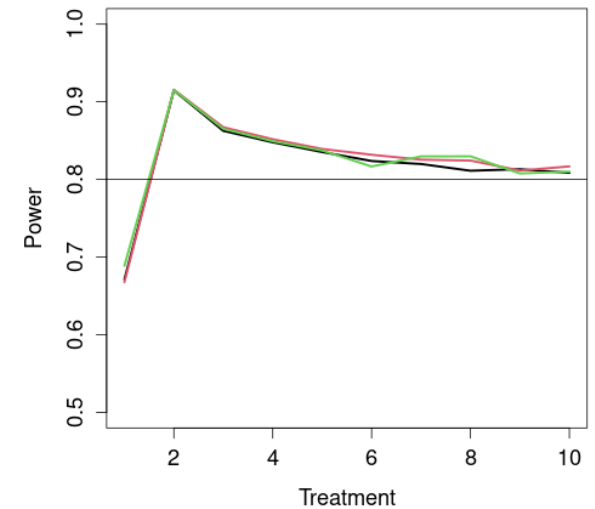


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# False Discovery Rate (FDR) control

- FDR control for platform trials (e.g, *Robertson et al 2019, 2022, Zehetmayer et al. 2022*)

$$\text{FDR} = E\left(\frac{V}{\max(R, 1)}\right)$$

- R: number of rejected hypotheses, V: number of wrongly rejected hypotheses
- However, conventional methods for FDR control assume that
  - Number of hypothesis tests is fixed
  - All p-values are available at time of test decision.
- **Online control of the FDR**

# Online control of the FDR

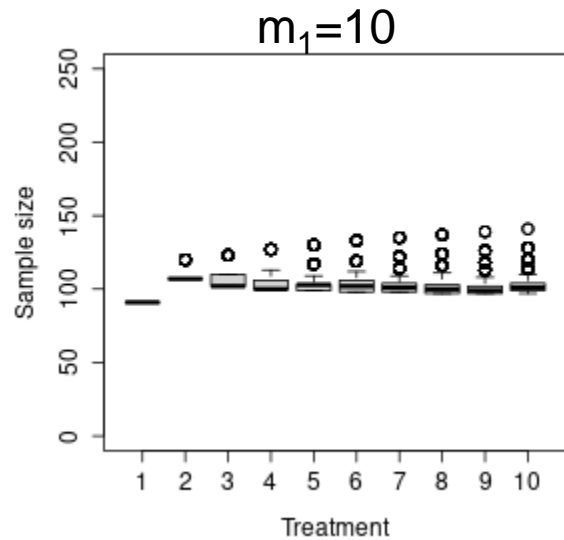
- Predefined order of hypotheses
- At each step a decision is made if the current  $H_i$  is rejected based on previous decisions.
- E.g., *Javanmard and Montanari, 15, 18*

## **LOND procedure** for online FDR control

- Decreasing significance levels  $\alpha_1, \alpha_2, \dots$  are allocated to sequence of null hypotheses  $H_1, H_2, \dots$
- In case of previous rejections, the significance levels are increased.

# Oracle scenario with online FDR control

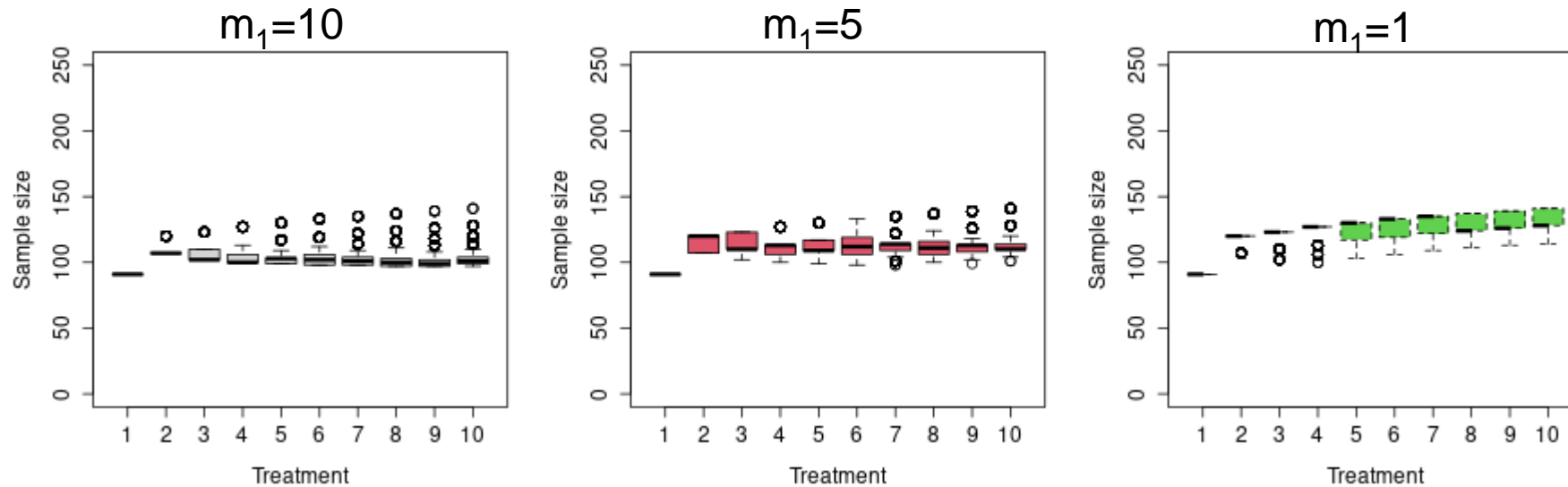
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- Allow for a total of **100** treatment arms



- Remember: For level- $\alpha$  tests, for each treatment  **$n=64$**  patients

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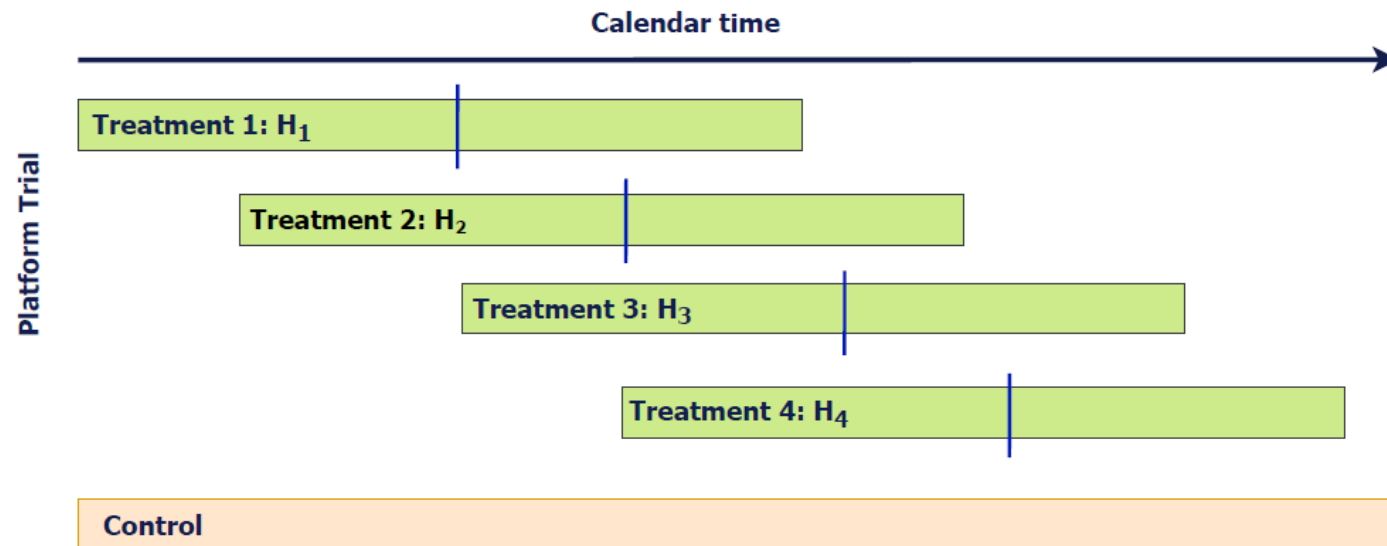


- Remember: For level- $\alpha$  tests, for each treatment  $n=64$  patients
- Sample sizes depend on  $m_1$  and the position of the treatment.



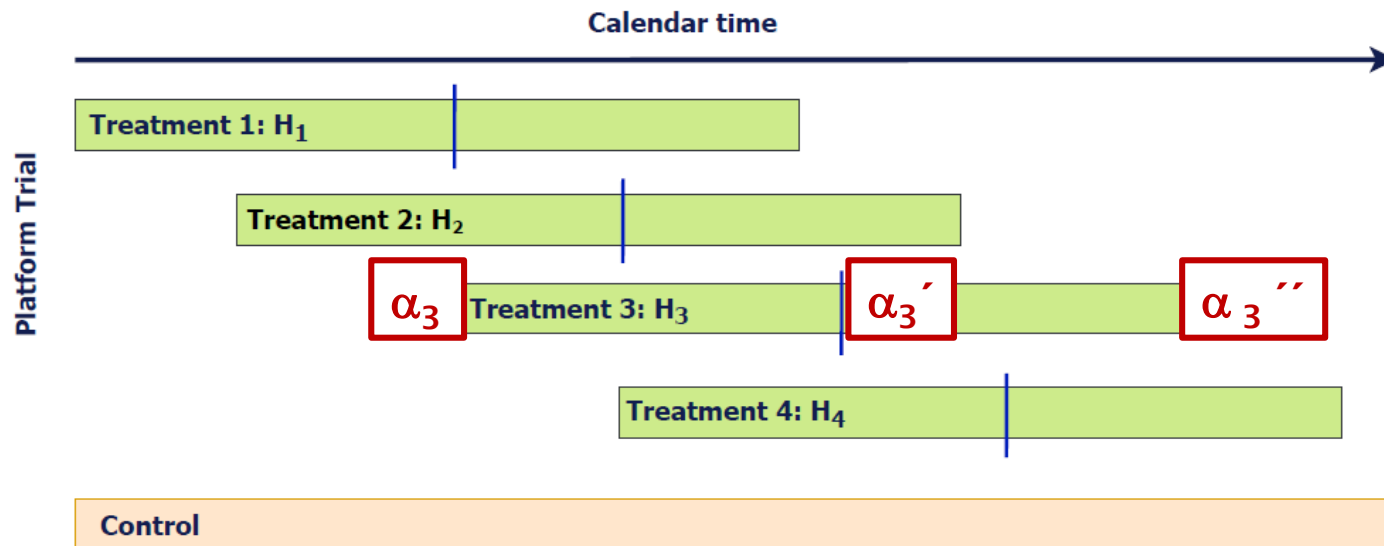
# Adaptive design

- In *Zehetmayer et al.*, 22 we considered a group-sequential LOND procedure (gsLOND) with the option to stop in the interim analysis.
- For gsLOND the significance level  $\alpha_i$  might be increased between interim and final analysis.
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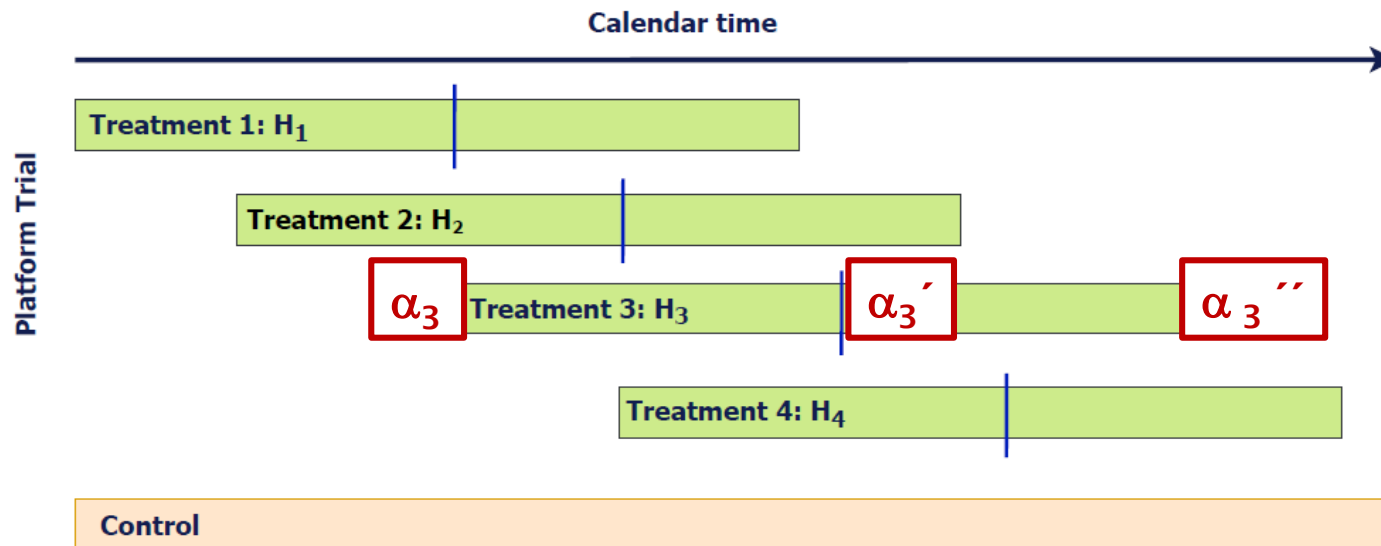


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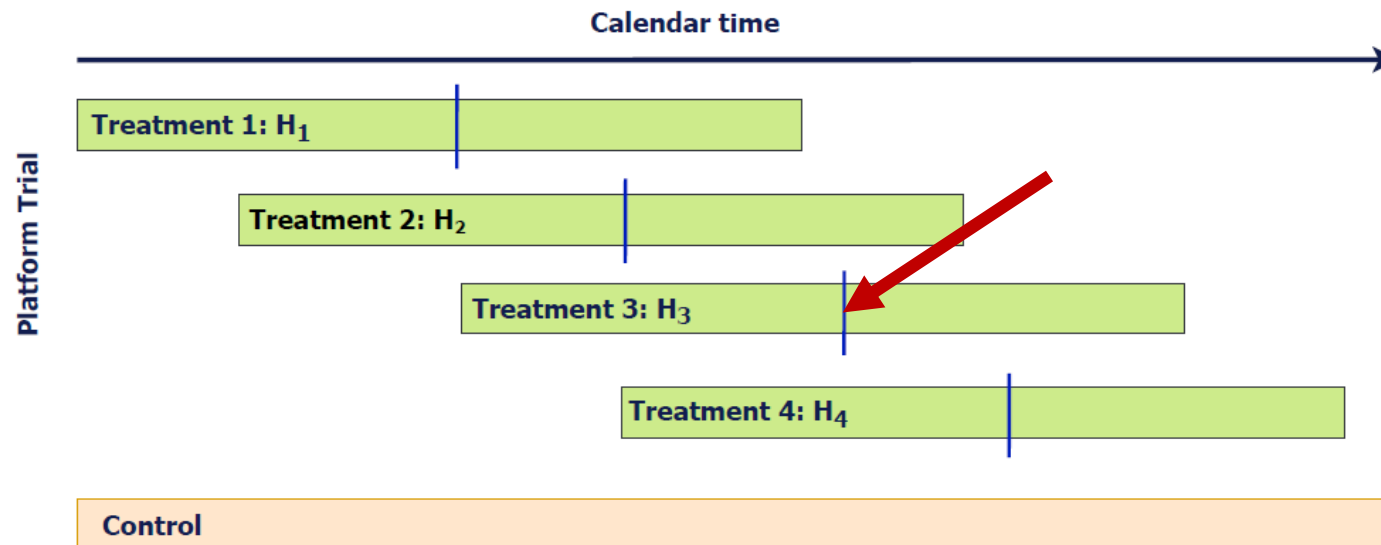
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**NOW:** In interim analysis:

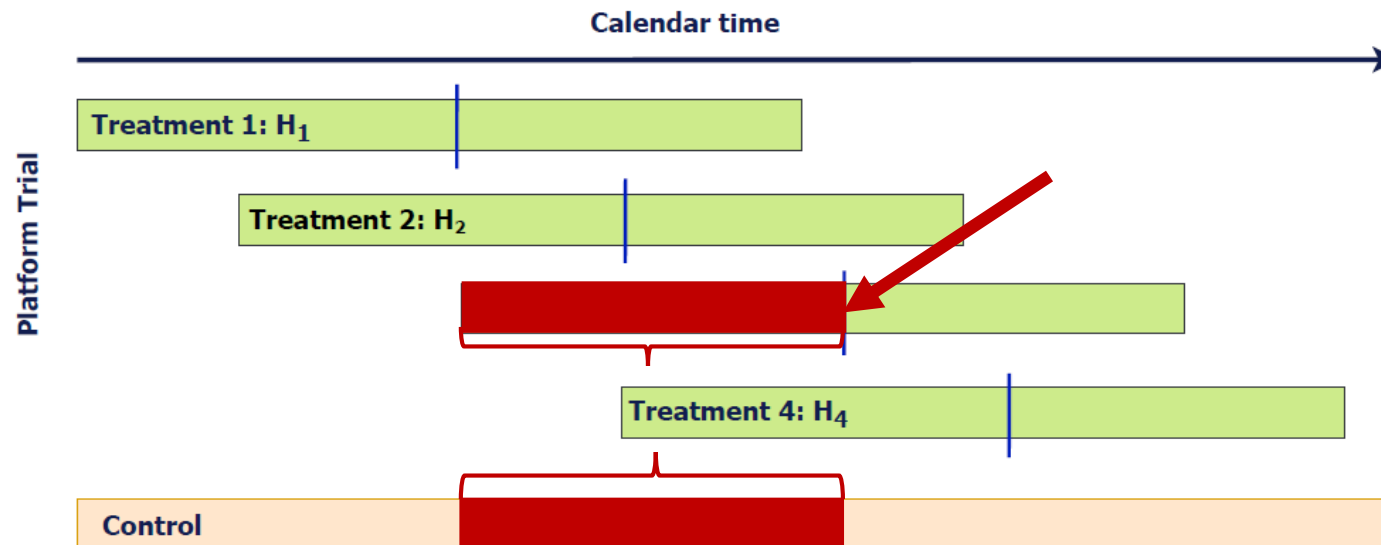
- Stopping for futility
- Efficacy stopping
- Update  $\alpha_i$
- Sample size reassessment with conditional error function for a conditional power of 0.8



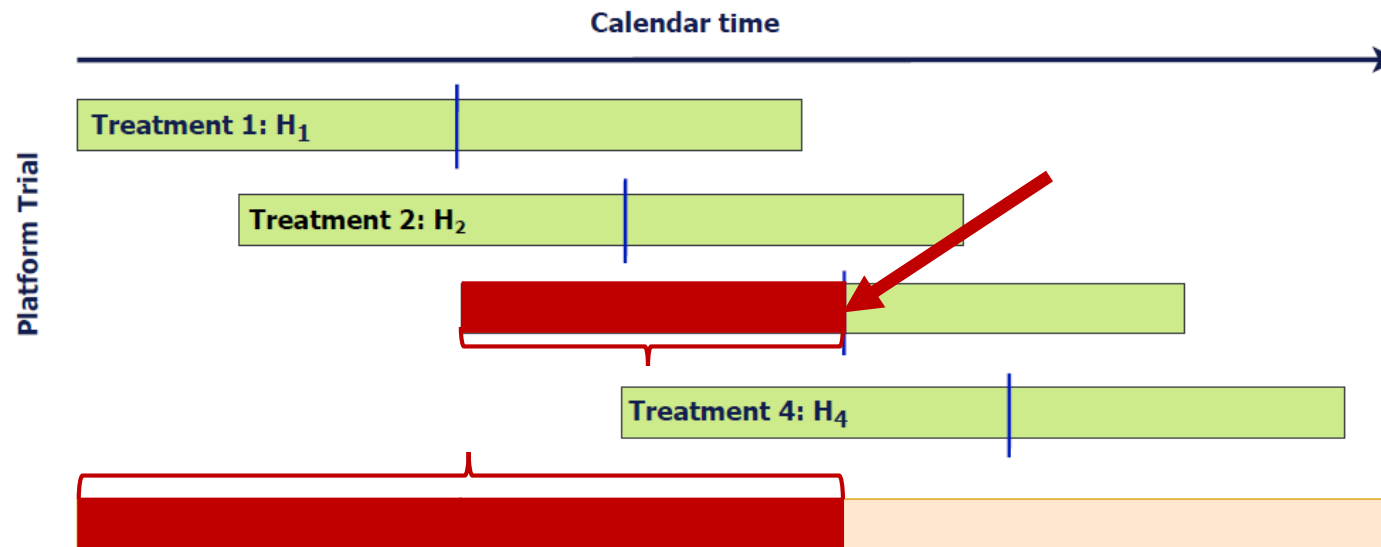
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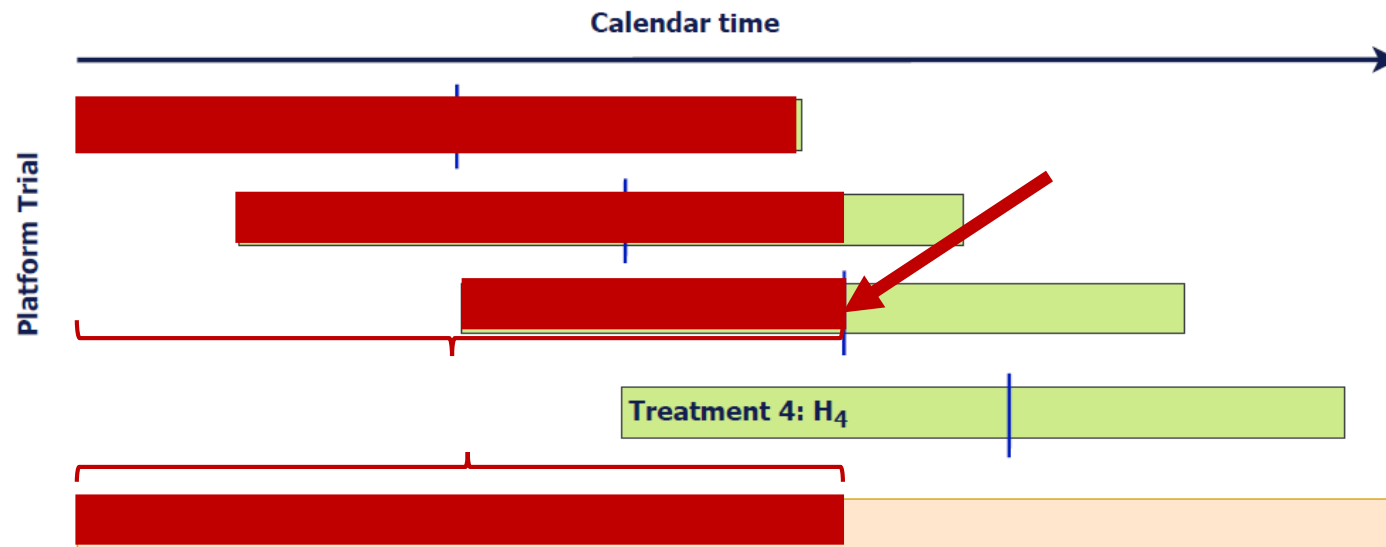
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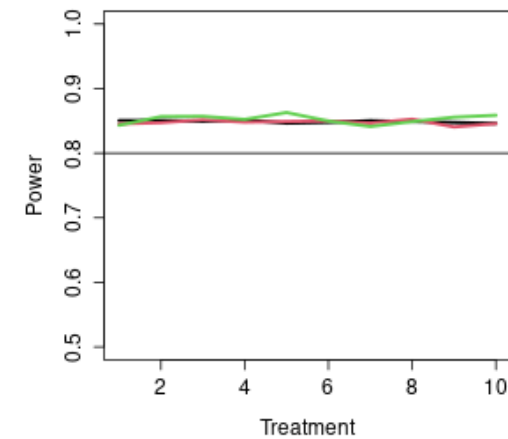
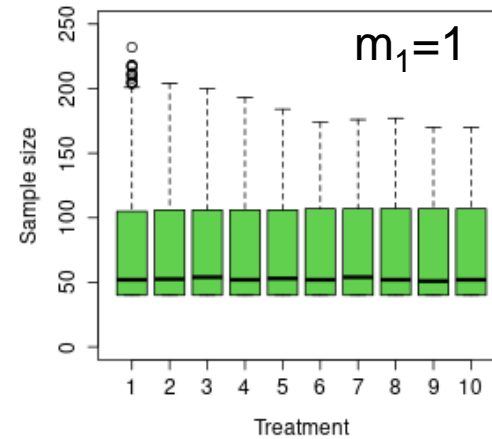
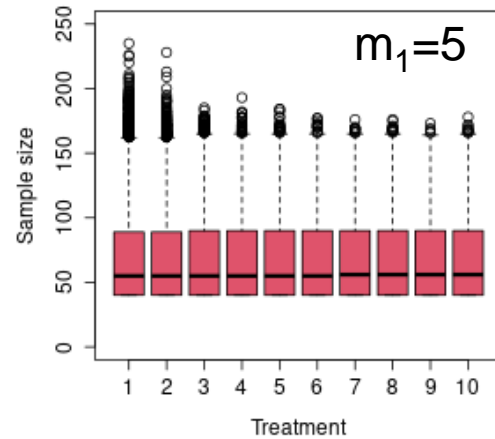
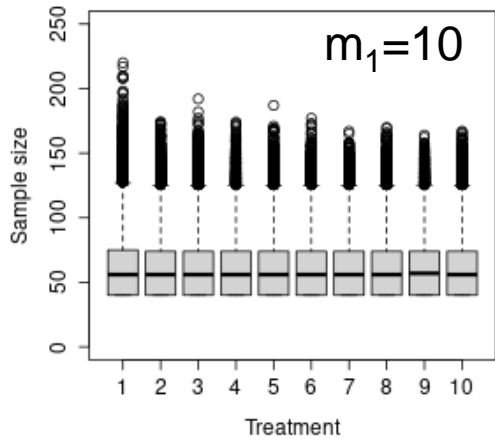
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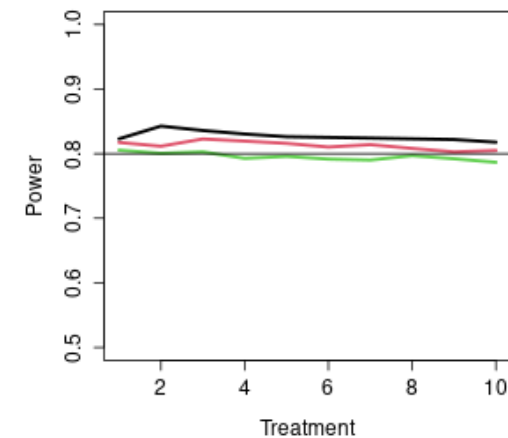
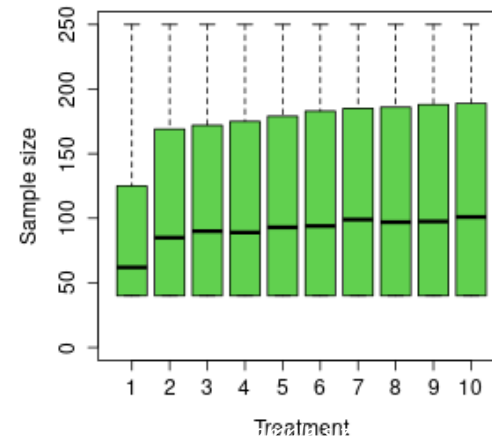
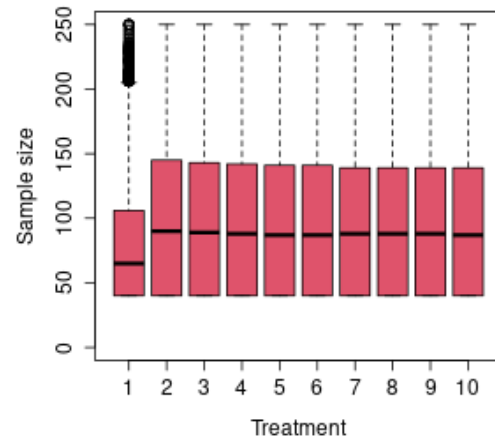
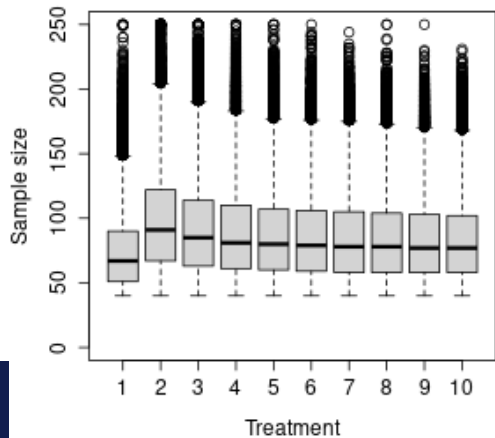
# Adaptive design with stopping for futility at $\alpha_1=0.5$

- O'Brien-Fleming design for inverse normal method, minimum sample size in stage 2 is 10.
- Estimate sd for sample size reassessment from all controls and interim data

## Level- $\alpha$ tests



## FDR





# Summary

- Benefiting from the past: The structure of platform trials helps to estimate sample sizes as past observations can be used in the planning phase.
  - Overlap of treatments has a high influence.
  - For very early treatments, planning is more difficult.
- **Sample size reassessment** might be a good choice.
  - Extension: reduction of influence of data from earlier treatments



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