# Optimal allocation strategies for platform trials

#### Marta Bofill Roig, Ekkehard Glimm, Tobias Mielke and Martin Posch

Adaptive Designs and Multiple Testing Procedures Workshop 2023



#### Acknowledgements

WP2 of Scientific, Regulatory and Operational Methodology

"Optimal allocation strategies in platform trials". (2023) M. Bofill Roig, E. Glimm, T. Mielke, and M. Posch. arXiv:2304.03035 [stat.ME]





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- Treatments to be studied not defined upfront
- Control arm can be shared

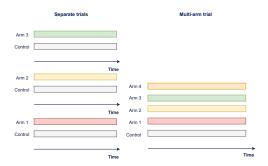
 $<sup>\</sup>mathbf{1}_{\rm Woodcock}$  & LaVange (2017). Master Protocols to Study Multiple Therapies, Multiple Diseases, or Both. NEJM

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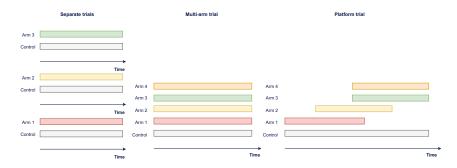
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### Optimal allocation of patients to treatment and control arms

In multi-arm trials with a shared control, further efficiency gains can be obtained by optimising the allocation rates of participants to the different treatment groups.

Optimal rates depend on the **optimisation criteria** and **analysis method**.

In platform trials,

- Optimal allocations to maximize the probability to find all treatments that are better than  ${\rm control.}^2$
- Optimal allocations to minimize the total sample size to achieve a desirable marginal power level.  $^3$

<sup>&</sup>lt;sup>2</sup>Bennett & Mander. (2020). Designs for adding a treatment arm to an ongoing clinical trial. Trials <sup>3</sup>Pan, Yuan & Ye. (2022). An Optimal Two-Period Multiarm Platform Design with New Experimental Arms Added During the Trial. The New England Journal of Statistics in Data Science

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**Time trends** are a concern in platform trials, when changing allocations over time and using non-concurrent controls.

• Adjusted analyses are recommended to avoid potential biases.

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Optimal allocations for trials considering time-adjusted analyses, and using concurrent data only or concurrent and non-concurrent data.

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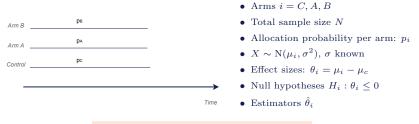
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Arm B	
Arm A	
Control	 -
-	

Time



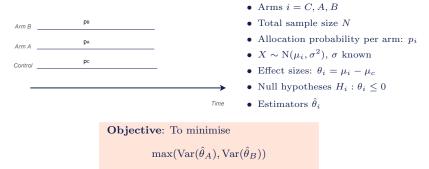
- Arms i = C, A, B
- Total sample size N
- Allocation probability per arm:  $p_i$
- $X \sim N(\mu_i, \sigma^2), \sigma$  known
- Effect sizes:  $\theta_i = \mu_i \mu_c$
- Null hypotheses  $H_i: \theta_i \leq 0$
- Estimators  $\hat{\theta}_i$



**Objective**: To minimise

 $\max(\operatorname{Var}(\hat{\theta}_A), \operatorname{Var}(\hat{\theta}_B))$ 

by means of optimising  $p_i$ 



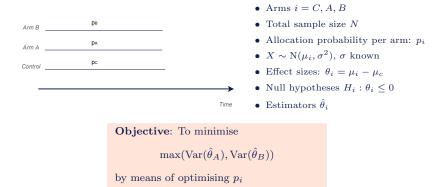
by means of optimising  $p_i$ 

In multi-arm trials with k treatment arms, the optimal allocation rates are

$$p_A = p_B$$
 and  $p_C/p_A = \sqrt{k}$ 

and then variances are equal. If k = 2

$$p_A = p_B = \frac{1}{2 + \sqrt{2}}$$
 and  $p_C = \frac{\sqrt{2}}{2 + \sqrt{2}}$ 



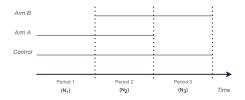
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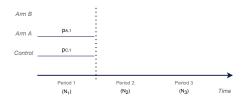
But, are these rates also optimal in platform trials?

Arm B			
Arm A		-	
Control	 		
			<b>→</b>

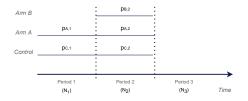
Time



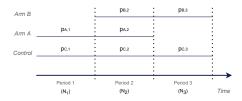
- Arms *i*, **periods** *s*
- $\bullet\,$  Sample sizes N and  $N_s$
- Allocation rates per arm and period: p<sub>i,s</sub>, ∑<sub>s</sub> p<sub>i,s</sub> = 1
- $X \sim N(\mu_i, \sigma^2), \sigma$  known
- Effect sizes:  $\theta_i = \mu_i \mu_c$
- Null hypotheses  $H_i: \theta_i \leq 0$
- Period stratified estimators  $\hat{\theta}_i$
- Concurrent controls only



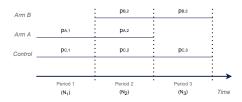
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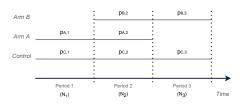


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**Objective**: To minimise

 $\max(\operatorname{Var}(\hat{\theta}_A), \operatorname{Var}(\hat{\theta}_B))$ 

by means of optimising  $p_{i,s}$ 



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**Objective**: To minimise

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Optimal allocations depend on the **trial design configuration** with respect to the sample sizes per period.

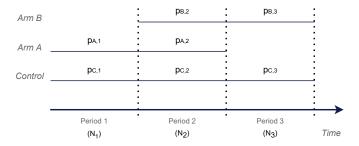
Also, under suitable conditions, the solution satisfies

•  $Var(\hat{\theta}_A) = Var(\hat{\theta}_B)$ 

#### Optimal allocations

For given entry time of Arm B and exit time of Arm A

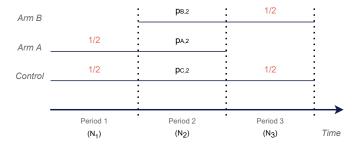
Assume  $N, N_1, N_2$  (and  $N_3$ ) are fixed and optimise  $p_{i,s}$ 



#### Optimal allocations

For given entry time of Arm B and exit time of Arm A

Assume  $N, N_1, N_2$  (and  $N_3$ ) are fixed and optimise  $p_{i,s}$ 



#### **Optimal allocations:**

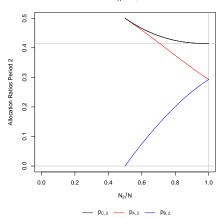
- Equal allocation between treatment and control arms in periods 1 and 3.
- No closed form solution for the optimal rates in **period 2**.
- Optimal rates in period 2 depend on  $N_1$  and  $N_2$ .

- The proportion of patients allocated to control in period 2,  $p_{C,2}$ , is greater or equal than  $p_{A,2}$  and  $p_{B,2}$ .
- The proportion p<sub>C,2</sub> is not monotone in N<sub>2</sub>, and it takes the minimum when N<sub>1</sub> = N<sub>3</sub>.
- If  $N_1 = N_3$ , then

$$p_{A,2} = p_{B,2} = \frac{1}{2 + \sqrt{2}}$$

and

$$p_C = \frac{\sqrt{2}}{2 + \sqrt{2}}$$



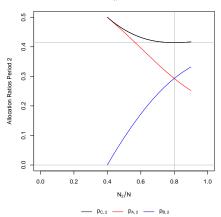
 $N_1/N = 0$ 

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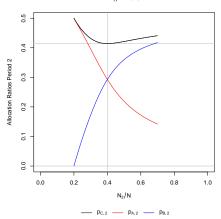
 $N_1/N = 0.1$ 

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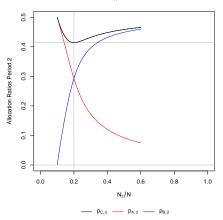
 $N_1/N = 0.3$ 

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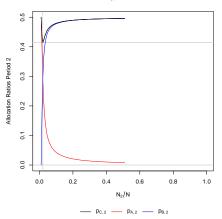
 $N_1/N = 0.4$ 

- The proportion of patients allocated to control in period 2,  $p_{C,2}$ , is greater or equal than  $p_{A,2}$  and  $p_{B,2}$ .
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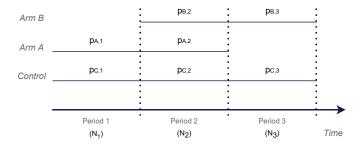
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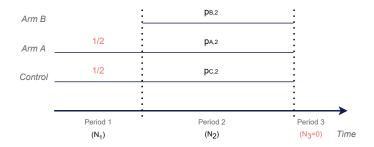
 $N_1/N = 0.49$ 

#### Optimal allocations depending on the trial design What if in addition optimise $N_2$ ?



Fix N and  $N_1$  and optimise  $p_{i,s}$  and  $N_2$ ,  $N_3$ 

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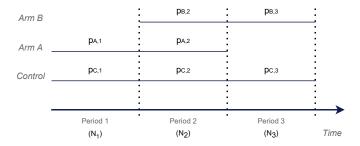
Fix N and  $N_1$  and optimise  $p_{i,s}$  and  $N_2$ ,  $N_3$ 

#### **Optimal allocations:**

- The solution leads to  $N_3 = 0$  and thus a **two-period trial**.
- The design is a particular case of the previous where  $N_2 = N N_1$ .

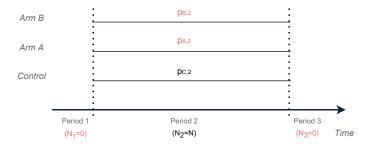
### Optimal allocations depending on the trial design With no restrictions on entry and exit times

Fix N and optimise  $p_{i,s}$  and the period sample sizes  $N_1, N_2, N_3$ 



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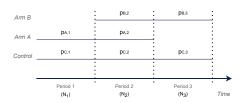
Fix N and optimise  $p_{i,s}$  and the period sample sizes  $N_1, N_2, N_3$ 



#### **Optimal allocations:**

- The solution leads to  $N_1 = N_3 = 0$  and thus a classical multi-arm trial.
- The optimal solution is  $p_{A,2} = p_{B,2}$  and  $p_{C,2}/p_{A,2} = \sqrt{2}$ .

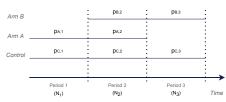
#### What about optimal rates if non-concurrent controls are used?



- Arms i, **periods** s
- Sample sizes N and  $N_s$
- Allocation rates per **arm and period**:  $p_{i,s}$
- $X \sim N(\mu_i, \sigma^2), \sigma$  known
- Effect sizes:  $\theta_i = \mu_i \mu_c$
- Null hypotheses  $H_i: \theta_i \leq 0$

<sup>&</sup>lt;sup>4</sup>Bofill Roig, M., Krotka, P., et al. (2022). On model-based time trend adjustments in platform trials with non-concurrent controls. BMC Medical Research Methodology.

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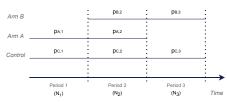
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#### Estimators

- Period stratified estimators  $\hat{\theta}_A$  using only concurrent controls.
- Period stratified estimators  $\tilde{\theta}_B$  using non-concurrent controls based on model adjustments.<sup>4</sup>

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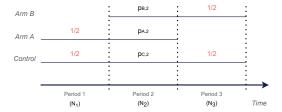
Under suitable conditions, the solution satisfies  $Var(\hat{\theta}_A) = Var(\tilde{\theta}_B)$ .

<sup>&</sup>lt;sup>4</sup>Bofill Roig, M., Krotka, P., et al. (2022). On model-based time trend adjustments in platform trials with non-concurrent controls. BMC Medical Research Methodology.

#### Optimal allocations for trials with non-concurrent controls

**Design 1:** Fix N,  $N_1$ ,  $N_2$  (and  $N_3$ ) and optimise  $p_{i,s}$ 

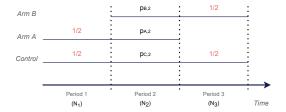
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#### Optimal allocations for trials with non-concurrent controls

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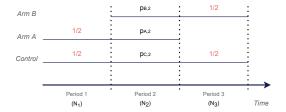
**Design 2:** Fix N and  $N_1$  and optimise  $p_{i,s}$  and the sample sizes  $N_2, N_3$ 

- The solution is a two-period trial with equal allocation in period 1.
- Particular case of Design 1 with  $N_2 = N N_1$ .

#### Optimal allocations for trials with non-concurrent controls

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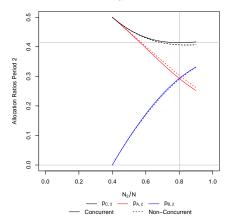
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#### **Design 3:** Fix N and optimise $p_{i,s}$ and the period sample sizes $N_1, N_2, N_3$

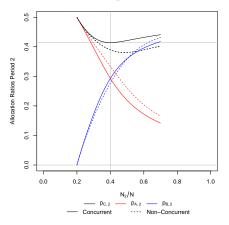
• The optimal solution is a multi-arm trial with  $p_{A,2} = p_{B,2}$  and  $p_{C,2}/p_{A,2} = \sqrt{2}$ .

- The pattern of the optimal allocation rates is similar to the trial with concurrent controls.
- The proportion of patients allocated to control in period 2,  $p_{C,2}$ , is lower when non-concurrent controls are used.
- The proportion p<sub>C,2</sub> may be lower than the proportion of patients assigned to arm 1 or 2, p<sub>A,2</sub> and p<sub>B,2</sub>.



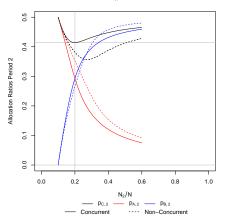
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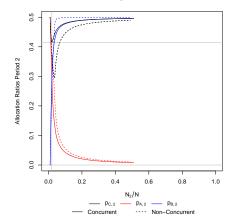
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 $N_1/N = 0.49$ 

#### Decrease in variance when using the optimal allocations

• Shiny app available at: https://github.com/MartaBofillRoig/Allocation

#### **Optimal Allocations in Platform Trials**

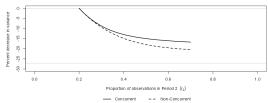


Concurrent

Optimal Allocation Ratios in Period 2



= Non-Concurrent



#### Conclusions

- The multi-armed trial (where all treatment arms enter at the start) is more efficient than platform trials with staggered entry of treatments, even when utilising non-concurrent controls.
- If treatments enter at later time points, the optimal allocation depends on the given entry times and all treatments continue to the very end of the platform trial to maximise the sharing of controls.
- In practice, the time a treatment is in the platform should be restricted and, for this case, a restricted optimisation can be performed.
- For two-arm three-period platform trials where the design is symmetrical with respect to sample sizes per period, the allocation in period 2 would be  $1:1:\sqrt(2)$
- If the entry time of Arm B is unknown, equal allocation will remain in the first period and the optimal allocation ratios for period 2 can be computed when Arm B enters the platform assuming the exit time of Arm A fixed.
- Other strategies and types of allocation could be considered, such as response-adaptive randomisation.

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## Thank you! gràcies eskerrik asko grazas gracias!



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